













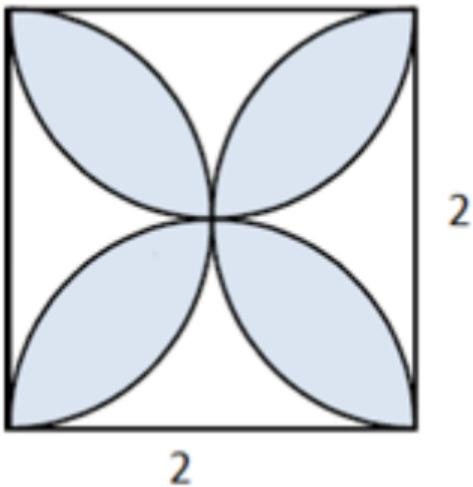






# Question 5

The figure shows a square and four semicircles generated with each side of the square as a diameter. If the side length of the square is 2, find the area of the shaded region.



# Solution 5

ANS: Area of the shaded region is  
 $2\pi - 4$



# Question 6

Amber, Ben, and Cathy shared a pizza. Amber ate  $\frac{1}{5}$  of the pizza, Ben ate one-half as much as Cathy did. Find how much of the pizza Ben ate



# Solution 6

$$\text{ANS: } \frac{4}{15}$$



# Question 7

If you select at random an integer number from 66 to 201, both included, what is the probability that the number is divisible by 2 or 3?



# Solution 7

$$\text{ANS: } \frac{91}{136} \approx 0.67$$



# Question 8

Let  $a$  and  $b$  be real numbers such that  $a \neq b$ ,  $a^2 + 3a = 2$ , and  $b^2 + 3b = 2$ .  
Find the value of  $(1 + a)(1 + b)$ .



# Solution 8

ANS: -4



# Question 9

Let  $z$  be a complex number such that  $z^5 = 1$  and  $z \neq 1$ . Compute

$$z + \frac{1}{z} + z^2 + \frac{1}{z^2}$$



# Solution 9

ANS: -1



# Question 10

$$\text{Let } f(x) = (2 - \sin \sqrt{x})^2$$

What is the maximum value of  $f(x)$ ?



# Solution 10

ANS: 9



# Question T1

In order to buy a book, Emma needed 7 more cents but Kim needed 1 more cent. They decided to combine their money but even then they did not have enough money to buy the book. How much did the book cost?



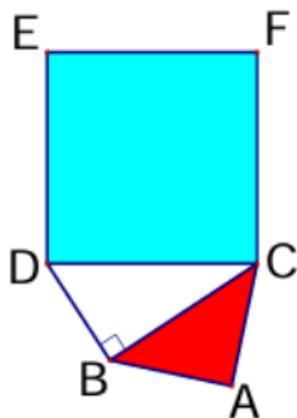
# Solution T1

ANS: 7



# Question T2

In the accompanying figure  $\triangle ABC$  is an isosceles right triangle with the right angle at  $A$  and each leg's length equals to 28 cm. The triangle  $\triangle DBC$  is a right triangle in which the leg  $BD$  is 21 cm. What is the area of the square  $DEFC$ ?



# Solution T2

ANS:  $2009\text{cm}^2$



# Question T3

If  $a$  and  $b$  are the solutions of the equation  $x^2 + 2019x - 2020 = 0$ . What is the value of

$$\frac{1}{a} + \frac{1}{b}$$



# Solution T3

$$\text{ANS: } \frac{-2019}{2020}$$



# Question T4

In the series  $a_n$ , every three consecutive terms are the edges of a right triangle with the last term the hypotenuse. For instance, if the first two terms are 3, and 4, then the third term will be 5, because 3, 4, 5 are the three edges of a right triangle. Assume  $a_1 = 3$ ,  $a_2 = 4$ . What is the length of the hypotenuse of the 10th right triangle according to the series?



# Solution T4

$$\text{ANS: } \sqrt{1919} = 43.81$$



# Question T5

Suppose  $z_1$ ,  $z_2$ , and  $z_3$  are the three roots of  $z^3 - 18z - 8 = 0$ . Simplify

$$A = \frac{(z_1 - z_2)^2(z_2 - z_3)^2(z_3 - z_1)}{200}$$



# Solution T5

$$\text{ANS: } A = 108$$



# Question T6

Find the value of  $x$  if

$$3^x - 2^x = \sqrt{6^x}$$







